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# Can Undoped Calcium Tetraborides Exist? An Answer from the Comparison of Its Density Functional Theory Electronic Structure with that of Rare-Earth Metal Tetraboride

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Periodic density functional theory calculations are used to discuss the existence of metal tetraborides  $MB_4$  with divalent metals. Tetraborides which contain metal atoms inserted in a three-dimensional boron network made of  $B_6$  octahedra and  $B_2$  dumbbells exhibit a pseudo energy gap for a count of 60 valence electrons per  $M_4(B_6)_2(B_2)_2$  formula unit. Such a count satisfies the stability electron requirement for  $B_6^{2-}$  (20 electrons) octahedra and  $B_2^{2-}$  (8 electrons) units and allows the filling of two supplementary low-lying bands deriving from the valence metallic d atomic orbitals. This favored electron count is not reached for CaB<sub>4</sub> which is then formally deficient by one electron per metal atom. This indicates that CaB<sub>4</sub> is unlikely to exist without *n*-doping.

#### Introduction

Borides of Group 1, 2, and 3 metals are known for exhibiting extended 2-dimensional (2D) or 3-dimensional (3D) networks of boron.<sup>1</sup> Typical examples are superconducting MgB<sub>2</sub> in which the boron atoms are arranged in graphite-like layers<sup>2</sup> and CaB<sub>6</sub> in which boron octahedra are linked to each other through intercluster B–B bonds in the three directions, forming a simple cubic packing.<sup>3</sup> It is often possible to rationalize the structural arrangement of these compounds in terms of simple electron counting rules within the ionic "Zintl–Klemm" bonding scheme, that is, assuming a fully oxidized metal cation sublattice interacting with an anionic boron network. For example, in MgB<sub>2</sub> [Mg<sup>2+</sup>(B<sup>-</sup>)<sub>2</sub>] the B<sup>-</sup> atoms satisfy the octet rule in the same manner as C does in graphite. Similarly, in CaB<sub>6</sub> [Ca<sup>2+</sup>(B<sub>6</sub>)<sup>2-</sup>] the (B<sub>6</sub>)<sup>2-</sup>

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octahedra satisfy the electron counting rules of the polyhedralskeletal-electron-pair (PSEP) theory,<sup>4</sup> with 7 skeletal electron pairs for intracluster bonding and 6 electrons (one on each boron atom) for making 6 intercluster localized 2-electron/ 2-center bonds.<sup>5</sup> Because both  $Ca^{2+}$  and  $(B_6)^{2-}$  satisfy the closed-shell requirement,  $CaB_6$  is a semiconductor at ambient pressure.<sup>6</sup> However, deviations away from these electroncounting rules can occur. For example, the conducting compounds  $KB_6^7$  and  $LaB_6$ ,<sup>8</sup> which are isostructural to  $CaB_6$ , are lacking and exceeding one electron per  $B_6$  unit, respectively, for satisfying the PSEP rules. In the former case, the

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**Figure 1.** ThB<sub>4</sub>-type crystal structure. Projections down (left) and along (right) the c axis. Large gray spheres and small black or gray spheres represent metal and boron atoms, respectively.

 $(B_6)^-$  octahedra tend to compensate their electron deficiency by forming bipolarons, that is, weak Jahn–Teller coupling between neighboring octahedra.<sup>7</sup> It has been claimed that KB<sub>6</sub> is stabilized by carbon insertion.<sup>8</sup> Interestingly, NaB<sub>6</sub> seems to be stable only when it is doped with a substantial amount of carbon to reach the NaB<sub>5</sub>C composition.<sup>8</sup> In LaB<sub>6</sub>, the excess electron is shared between the B<sub>6</sub> units and La, thus leading to a metal formal charge intermediate between +2 and +3.<sup>9</sup>

Metal Tetraborides. Electron Counting Considerations. Tetragonal (P4/mbm) rare-earth metal tetraborides of the  $ThB_4^{10,11}$  structure-type have a somewhat more complicated architecture. They also contain B6 octahedra, but in that case they are directly bonded to each other only in the c direction. In the ab plane, the B<sub>6</sub> octahedra are linked to each other through B<sub>2</sub> units (see Figure 1). These units are made of sp<sup>2</sup>-hybridized boron atoms (labeled B3 in Figure 1), each of them being bonded to two B<sub>6</sub> octahedra and to its partner in the B3-B3 unit. The three corresponding bond lengths are of the same order of magnitude ( $\sim 1.7 - 1.8$  Å). Therefore,  $MB_4$  (M = rare-earth metal) can be reformulated  $M_2(B_6)(B_2)$ . The question which arises then is the formal charge distribution between M, the B<sub>6</sub>, and the B<sub>2</sub> units. While a charge of 2- can easily be attributed to the B<sub>6</sub> octahedron by analogy with CaB<sub>6</sub>, the charge attribution for the B<sub>2</sub> units is not so straightforward. Assuming localized 2-electron/2-center bond-

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ing around these atoms leads to three possible electron counts, each corresponding to one of the Lewis formulas given in Scheme 1. The bonding scheme depicted in Scheme 1*a* is satisfactory from the point of view of boron bonding because it corresponds to planar tricoordinated atoms obeying the sextet rule, a situation not uncommon in boron molecular chemistry.<sup>12</sup> However, it is less satisfactory from the point of view of the formal charge balance, that is,  $(M^+)_2(B_6^{2-})(B_2)$ because it leaves a generally trivalent metal in an unrealistically low oxidation state. The situation in Scheme 1b exhibits negatively charged sp<sup>2</sup>-hybridized boron atoms which satisfy the octet rule. The charge partitioning  $(M^{2+})_2(B_6^{2-})(B_2^{2-})$  is more realistic for M, but the B3–B3 interatomic distance does not show a strong tendency for multiple bonding in any of the structurally characterized compounds of this type.<sup>10,11</sup> The charge partitioning associated with Scheme 1c,  $(M^{3+})_2(B_6^{2-})(B_2^{4-})$ , corresponds to a fully oxidized metal, a B3-B3 single bond, and B3 atoms satisfying the octet rule. However, in such a situation the sp<sup>2</sup> hybridization of boron should be disfavored over the nonplanar sp<sup>3</sup> one. Moreover, the coexistence in the same structure of particularly electronrich B<sup>2-</sup> atoms, bearing a nonbonding lone-pair, with electron-poor  $B_6^{2-}$  clusters does not look *a priori* reasonable. Thus, none of the charge partitioning is at first sight fully satisfactory. Previous tight-binding calculations on GdB<sub>4</sub> carried out in our group at the extended Hückel level concluded that the Lewis formula (Scheme 1b) is the one which provides the best description of the bonding in this compound.<sup>11</sup> It was suggested that the formal B3=B3 double bond was particularly weak because of its coordination to the Gd atoms.

From these results, it appears reasonable to describe  $GdB_4$  (or any rare-earth metal tetraboride) as an electron-rich compound with respect to a hypothetical semiconducting

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### Undoped Calcium Tetraborides

CaB<sub>4</sub> compound, in the same way as LaB<sub>6</sub> is electron-rich relatively to the well-known semiconducting CaB<sub>6</sub> compound. It turns out that recently Meyer et al. published the synthesis and characterization of a carbon-doped calcium tetraboride (CaB<sub>4-x</sub>C<sub>x</sub>) in which the carbon content *x* is lower than 5%.<sup>13</sup> According to these authors, "upon first glance, it could be assumed that carbon may have a stabilizing effect... This simple consideration does not, however, satisfy the distinct bonding requirements with cations...". In other words, it has not been possible to synthesize pure CaB<sub>4</sub> so far. However, the extended Hückel tight-binding calculations carried out by the same authors on pure CaB<sub>4</sub> show a small but clear band gap at the Fermi level, confirming the stable closed-shell configuration associated with the (Ca<sup>2+</sup>)<sub>2</sub>(B<sub>6</sub><sup>2-</sup>)-(B<sub>2</sub><sup>2-</sup>) formal charge partitioning.<sup>13</sup>

Density functional theory (DFT) calculations were carried out on YB<sub>4</sub>, GdB<sub>4</sub>, and hypothetical CaB<sub>4</sub> to first check the validity of our previous tight-binding study on GdB<sub>4</sub><sup>11</sup> and then investigate the stability of hypothetical CaB<sub>4</sub>. The main results are reported here.

#### **Computational Details**

Self-consistent ab initio band structure calculations of MB4 were performed with the scalar relativistic tight-binding linear muffintin orbital method in the atomic spheres approximation including the combined correction (LMTO).14 Exchange and correlation were treated in the local density approximation using the von Barth-Hedin local exchange correlation potential.<sup>15</sup> Within the LMTO formalism, interatomic spaces are filled with interstitial spheres. Because of the closed packed character of the MB<sub>4</sub> crystallographic structure, no interstitial "empty" spheres were added. The full LMTO basis set consisted of 6s, 6p, 5d, and 4f functions for Gd spheres, 5s, 5p, 4d, and 4f functions for Y spheres, 4s, 4p, and 3d functions for Ca spheres, and 2s, 2p, and 3d functions for B spheres. Unless specified, the eigenvalue problem was solved using the following minimal basis set obtained from Löwdin downfolding technique: Gd (6s, 5d, 4f), Y (5s, 4d), Ca (4s, 3d), and B (2s, 2p). The k space integration was performed using the tetrahedron method.<sup>16</sup> Charge self-consistency and the average properties for GdB<sub>4</sub>, YB<sub>4</sub>, and  $CaB_4$  were obtained from 96 irreducible k points. The density of states (DOS) and crystal orbital Hamiltonian population (COHP)<sup>17</sup> curves were shifted so that the Fermi level lies at 0 eV. The electron localization function (ELF) was evaluated according to ref 18 within the TB-LMTO-ASA program package. To get more insight into the chemical bonding, ELF was analyzed with the program Basin.<sup>19</sup> An integration of the valence electron density in the basins defined by surfaces of zero flux in ELF gradient gave, analogously to the

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procedure proposed by Bader for the electron density,<sup>20</sup> the electron counts for each basin, which are important for the description of the bonding situation.

Full optimizations of the atomic positions and cell parameters were carried out on MB<sub>4</sub> using the Vienna Ab initio Simulation package (VASP).<sup>21</sup> Ion cores were represented by projector augmented wave (PAW) pseudopotentials provided within the program.<sup>22</sup> The Perdew–Burke–Ernzerhof (PBE) generalized gradient approximation (GGA) was employed for the exchange and correlation energy term.<sup>23</sup> The Brillouin zone was sampled using a  $8 \times 8 \times 16$  Monkhorst–Pack grid. A plane wave basis set with a cutoff energy of 600 eV was used to construct the valence electronic wave functions.

Phonon calculations were performed using the direct approch.<sup>24</sup> A displacement of 0.015 Å was used to move the atoms from their equilibrium position and then to calculate the Hessian matrix. The eigenvalues (frequencies) were obtained by diagonalizing the dynamical matrix.

Experimental and optimized crystallographic parameters, as well as the corresponding bond distances of  $MB_4$  compounds (M = Y, Gd, Ca) are shown in Table 1.

#### Discussion

Electronic Structure of the Anionic Boron Network. We start the analysis by looking at the electronic structure of the anionic  $(B_4)^{2-}$ , that is,  $[(B_6)(B_2)]^{4-}$  3D sublattice of CaB<sub>4</sub> which was computed using the artifact of removing all the functions centered on calcium atoms leading to a total transfer of their two valence electrons to the boron network. The total DOS shows a gap of about 1.6 eV for the 2– charge. Of interest is the projected DOS of B3, the boron atoms of the B<sub>2</sub> dumb-bells, shown in Figure 2. The highest occupied band and the lowest vacant one are dominantly B3(2p<sub> $\pi$ </sub>) in character. The B3–B3 COHP curve shows that the former is bonding and the latter antibonding. This is indicative of the existence of a B3=B3 double bond, at least in the isolated hypothetical  $[(B_6)(B_2)]^{4-}$  sublattice.

Electronic Structure of the Rare-Earth Metal Tetraborides. The total and projected DOS of  $MB_4$  are shown in Figure 3 and 4 for M = Y and Gd, respectively. For both compounds, the shape of the total DOS exhibits a deep minimum (close to zero) at the Fermi level. In other words, the pseudogap at the Fermi level corresponds to 2 more electrons per Gd<sub>2</sub>(B<sub>6</sub>)(B<sub>2</sub>) formula than that corresponding to formally (B<sub>6</sub>)<sup>2–</sup> and (B<sub>2</sub>)<sup>2–</sup> units. This may suggest (B<sub>2</sub>)<sup>4–</sup> rather than (B<sub>2</sub>)<sup>2–</sup> units. Otherwise, assuming (B<sub>2</sub>)<sup>2–</sup> units (thus  $M^{2+}$ metals) one may have expected a more "metallic-like" DOS shape, with a significant metal contribution at the Fermi level. Although the projections on the metal are consistent with a high oxidation state, in both cases they show a significant metal

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Table 1. Experimental and Computed Cell Parameters and Bond Distances in Some MB<sub>4</sub> Compounds <sup>a</sup>

	structure									
	YB <sub>4</sub> (exp.) <sup>10d</sup>	YB <sub>4</sub> (calc.)	GdB <sub>4</sub> (exp.) <sup>11</sup>	GdB <sub>4</sub> (calc.)	CaB <sub>3.75</sub> C <sub>0.25</sub> (exp.) <sup>13</sup>	CaB <sub>4</sub> (calc.)				
a (Å)	7.111 (3)	7.111	7.1316 (2)	7.137	7.0989 (7)	7.158				
<i>c</i> (Å)	4.017 (2)	4.029	4.0505 (2)	4.047	4.1353 (5)	4.095				
volume (Å <sup>3</sup> )	203.1 (2)	203.7	206.01 (1)	206.2	208.40 (4)	209.8				
Bonds (Å)										
$M-M^b$	3.663 (2)	3.660	3.682(1)	3.689	3.637	3.694				
	4.000(2)	4.029	4.051 (1)	4.047	3.682	3.766				
$M-B^b$	2.728 (4)	2.732	2.738 (2)	2.740	2.738 (1)	2.745				
	2.850(2)	2.858	2.873 (2)	2.876	3.142 (2)	3.090				
B1-B1	1.622 (4)	1.640	1.64 (1)	1.650	1.697 (4)	1.685				
B1-B2	1.747 (3)	1.752	1.759 (5)	1.756	1.773 (2)	1.758				
B2-B2	1.810(3)	1.813	1.815 (6)	1.816	1.822 (2)	1.811				
B2-B3	1.721 (3)	1.720	1.729 (5)	1.728	1.729 (2)	1.749				
В3-В3	1.752 (3)	1.747	1.75 (1)	1.757	1.670 (5)	1.729				

<sup>a</sup> See Figure 1 for boron atom numbering. <sup>b</sup> Range.



**Figure 2.** (a) Total DOS of the  $[(B_6)(B_2)]^{4-}$  sublattice, (b) total atomic DOS of B3, (c)  $B3(2p_{\pi})$  projected DOS, and (d)  $B3(2p_{\pi})-B3(2p_{\pi})$  COHP in the  $[(B_6)(B_2)]^{4-}$  sub-lattice.

participation to the occupied states. Indeed, the metallic character is rather homogeneously dispersed over a large energy range below the Fermi level. Similar results were reported for YB<sub>4</sub> by Herzig and co-workers.<sup>25</sup>

The projected DOS of the B3( $2p_{\pi}$ ) atomic orbitals of YB<sub>4</sub> are shown in Figure 5a. It corresponds to an occupation slightly below 50%. The B3( $2p_{\pi}$ )-B3( $2p_{\pi}$ ) COHP curve, which is shown in Figure 5b indicates that all the occupied B3( $p_{\pi}$ ) states are bonding, whereas most of the vacant states are antibonding. This is consistent with the existence of a  $\pi$  bond between the B3 atoms which is partly delocalized over the metals, *i.e.*,  $\pi$  donation to the metal depopulates the bonding B3( $2p_{\pi}$ ) states which mix somewhat with the empty metallic states.

The integrations of the various B-B COHP curves over the occupied states (ICOHP) are given in Table 2 for  $YB_4$ 



**Figure 3.** Total DOS and projected DOS of YB<sub>4</sub>: (a) total, (b) Y projection, and (c) B3 contribution.

and GdB<sub>4</sub>. Although such values cannot be compared between different compounds, they exhibit similar trends within each compound. As expected, the values corresponding to the bonds inside the electron-deficient B<sub>6</sub> octahedron are significantly lower than the values corresponding to the other bonds which are localized. Among the latter, the shorter one, that is, the interoctahedra bond, appears to be the strongest. This is likely due to hyperconjugation between neighboring octahedra. It is noteworthy that the weakest of the three localized bonds is B3–B3 in both compounds. Clearly, the formally B3=B3 double bond is particularly weak, mainly because of the B3–B3  $\pi$  electron donation to the metal. Thus, the Lewis formula in Scheme 1*b* should be corrected by resonant structures such as those shown in Scheme 2.

The existence of a weak double bond is also ascertained by an ELF analysis.<sup>18</sup> A plot of this function ( $\eta = 0.8$ ), shown in Figure 6 for both compounds, exhibits around the

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**Figure 4.** Total DOS and projected DOS of  $GdB_4$ : (a) total, (b) Gd projection, and (c) B3 contribution.



**Figure 5.** (a) Projected DOS of the B3( $2p_{\pi}$ ) atomic orbitals and (b) B3( $2p_{\pi}$ )-B3( $2p_{\pi}$ ) COHP of YB<sub>4</sub>.

Table 2. ICOHPs and Basin Charges in YB4, GdB4, and CaB4 a

e									
	$YB_4$		GdB <sub>4</sub>		CaB <sub>4</sub>				
bond	ICOHP	charge	ICOHP	charge	ICOHP	charge			
B1-B2	0.6	12.3	0.6	12.0	0.6	12.0			
B2-B2									
B3-B3	0.9	3.8	0.9	3.9	1.0	3.0			
B1-B1	1.1	2.4	1.2	2.4	1.1	2.3			
B2-B3	1.0	2.5	1.0	2.5	1.0	2.5			

 $^a$  B–B ICOHPs are compared to B2–B3 ICOHPs which are arbitrarily set at one.

B3–B3 bond an envelope shape which resembles more that of a typical double bond rather than that of a single bond as it is around the B2–B3 and B1–B1 contacts. Basin integrated charges support this statement (Table 2). The charge computed for the whole  $B_6$  octahedron is very close



to the count of 20 electrons expected for a  $B_6^{2-}$  cluster. The charge computed for the stronger (and shorter) B1–B1 bond is smaller than that found for the B2–B3 and B3–B3 bonds. The latter value is close to 4, the ideal number for a double bond. The two former values are somewhat larger than the ideal value of 2 corresponding to a single bond, indicative of some hyperconjugation and  $\pi$  conjugation, respectively. Thus, all the results are consistent with the  $(M^{2+})_2(B_6^{2-})$ - $(B_2^{2-})$  charge partitioning, that is, the existence of one electron per metal atom lying in a d-type band. Interestingly, however, there is an unexpected pseudogap at the Fermi level which would fit better with the  $(M^{3+})_2(B_6^{2-})(B_2^{4-})$  charge partitioning.

**Electronic Structure of Undoped CaB**<sub>4</sub>. What about undoped CaB<sub>4</sub>? The total and projected DOS of CaB<sub>4</sub> are shown in Figure 7. Contrarily to the total DOS computed at the extended Hückel level by Meyer et al.,<sup>13</sup> the DFT one does not show any gap or pseudo gap at the Fermi level.



Figure 6. ELF plot of the B3–B3 bond for  $YB_4$  (top),  $GdB_4$  (middle), and  $CaB_4$  (bottom).



**Figure 7.** Total DOS and projected DOS of CaB<sub>4</sub>: (a) total, (b) Ca projection, and (c) B3 contribution.



Figure 8. Total DOS of CaB<sub>4</sub> without Ca d states.

Rather, a pseudo gap arises for a Fermi level which would correspond to (almost) one extra electron per CaB<sub>4</sub> repeat unit and thus to the electron count of YB<sub>4</sub> or GdB<sub>4</sub>. When the 3d atomic orbitals of Ca are not taken into account in the calculations, the pseudo gap adjusts to the Fermi level (Figure 8), quite similarly to the extended Hückel calculations of Meyer et al.<sup>13</sup> It turns out that in the  $MB_4$  series (M = Y, Gd, Ca), the low lying bands below the pseudo gap are associated with occupied levels of the  $B_6^{2-}$  and  $B_2^{2-}$  units, as well as what corresponds approximately to two metallic d-bands (per  $M_4B_{16}$  formula, the content of the unit cell). These low-lying metallic bands mix strongly with the boron ones. Consequently, they are difficult to identify. Nevertheless, the bands close to the Fermi level exhibit a large metallic character, as it can be seen on the fat-band structures of YB<sub>4</sub> and CaB<sub>4</sub> shown in Figure 9. This representation shows that these two supplementary bands lie below the pseudo gap. Clearly, extended Hückel tight-binding calculations, which usually do not use d-orbitals in the basis set for Ca, are unable to reproduce the pseudogap corresponding to 15 valence electrons per  $MB_4$  repeat unit.

The projected DOS of the  $B3(2p_{\pi})$  atomic orbitals of CaB<sub>4</sub> and the corresponding  $B3(2p_{\pi})-B3(2p_{\pi})$  COHP curve (Figure 10) resemble those of YB<sub>4</sub>. Thus, the electronic structures of CaB<sub>4</sub> and YB<sub>4</sub> are related, except



Figure 9. d-Type fat-band structures of  $CaB_4$  (top) and  $YB_4$  (bottom).



**Figure 10.** (a) Projected DOS of the  $B3(2p_{\pi})$  atomic orbitals and (b)  $B3(2p_{\pi})-B3(2p_{\pi})$  COHP of CaB<sub>4</sub>.

that CaB<sub>4</sub> has one less electron. The shape of the ELF plot ( $\eta = 0.8$ ) (Figure 6, bottom) is less characteristic of a double bond than that of YB<sub>4</sub>. Basin integrated charges (Table 2) indicate a B3–B3 value lower than 4. Clearly, the electron-deficiency of CaB<sub>4</sub> with respect to YB<sub>4</sub> is shared on the metal and B3 atoms.

#### Undoped Calcium Tetraborides

Phonon vibrations were computed at the  $\Gamma$  point in the Brillouin zone on the optimized structures of CaB<sub>4</sub> and YB<sub>4</sub>. Interestingly, the results show that for the former, the calcium compound, a dozen of imaginary frequencies are obtained varying from 80i to 680i cm<sup>-1</sup>, whereas for the latter, the yttrium compound, the imaginary frequencies do not exceed 3i cm<sup>-1</sup>, a value much lower than the computational accuracy limit. These results support the idea that undoped CaB<sub>4</sub> is not stable.

Carbon Position in the Carbon-Doped Phase CaB<sub>3.75</sub>-C<sub>0.25</sub>. The B3-B3 bond distance is 1.670 Å in the carbondoped phase  $CaB_{3.75}C_{0.25}$ .<sup>13</sup> It is significantly shorter than the corresponding bond distance generally measured in other metal tetraborides which are about 1.75 Å (see Table 1). This might indicate that the C atoms occupy the B3 position. This is supported by theoretical calculations carried out on CaB<sub>3.75</sub>C<sub>0.25</sub> (Ca<sub>4</sub>B<sub>15</sub>C). Indeed Ca<sub>4</sub>B<sub>15</sub>C was optimized at the DFT level of theory with carbon located in the B1 and B2 positions of the octahedra as well as in the B3 position in the  $B_2$  units (see Figure 1). The structure with carbon in the latter position is largely more stable than the other two structures with carbon located in B1 and B2 positions by 1.00 and 0.85 eV per Ca<sub>4</sub>B<sub>15</sub>C formula, respectively. B3-C and B3-B3 distances of 1.626 and 1.682 Å are computed for this structure, and its cell parameters fit well with those determined experimentally. This leads to an averaged distance of 1.668 Å, close to the "B3-B3" distance measured experimentally by Meyer for  $CaB_{3.75}C_{0.25}$  (1.670 Å)<sup>13</sup> and substantially shorter than the B3–B3 distance of 1.729 Å computed for CaB<sub>4</sub>.

## Conclusion

DFT calculations show that compounds with the ThB<sub>4</sub>type structure (including CaB<sub>4</sub>) exhibit a pseudo gap for a count of 60 valence electrons per  $M_4(B_6)_2(B_2)_2$  formula unit. This count satisfies the stability electron requirement for B<sub>6</sub><sup>2-</sup> (20 electrons) and B<sub>2</sub><sup>2-</sup> (8 electrons, see Scheme 1) units and allows the filling of two supplementary low-lying bands deriving from the valence metallic d atomic orbitals. This favored electron count is not reached for CaB<sub>4</sub> which is deficient by one electron per metal atom. This is likely the reason why only carbon-doped CaB<sub>4</sub> materials have been characterized so far. This raises the question of the existence of undoped CaB<sub>4</sub>, whereas CaB<sub>3</sub>C would possess the "ideal" electron count encountered in trivalent rare-earth metal tetraborides.

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